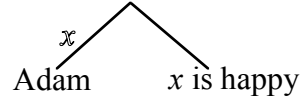
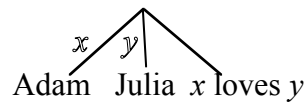


# Representing Propositional Structures with Trees

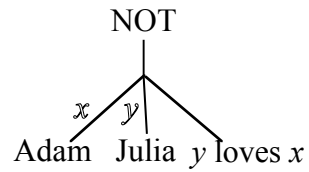
Adam is happy.



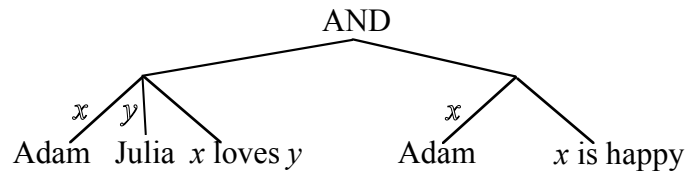
Adam loves Julia.



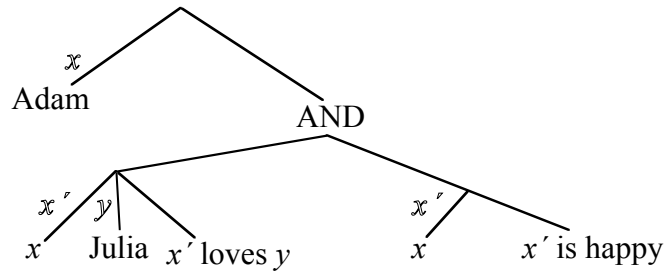
Julia does not love Adam.



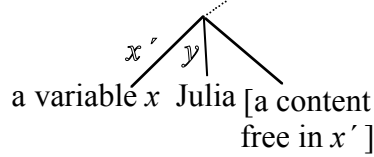
Adam loves Julia and Adam is happy.



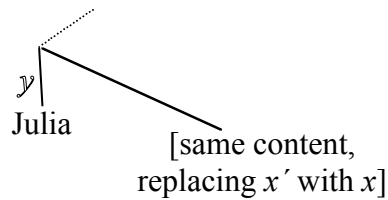
Adam loves Julia and is happy.  
 $[ \exists x(x \text{ loves Julia and } x \text{ is happy}) (\text{Adam}) ]$



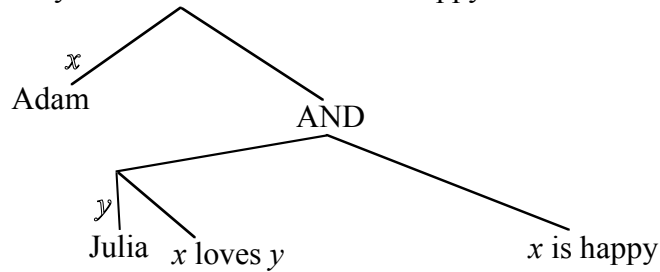
In general, whenever we have a structure of the form:



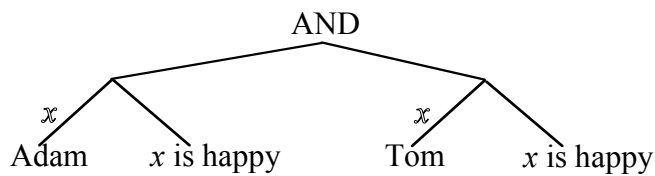
that will be equivalent to:



I will usually employ the second, simpler representation. Written that way, the proposition expressed by “Adam loves Julia and is happy” is:

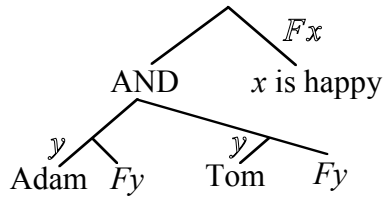


Adam is happy and Tom is happy.



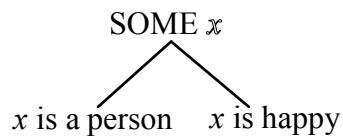
Adam and Tom are each happy.

[  $\forall x(F(\text{Adam is } F \text{ and Tom is } F) (x \text{ is happy}))$  ]



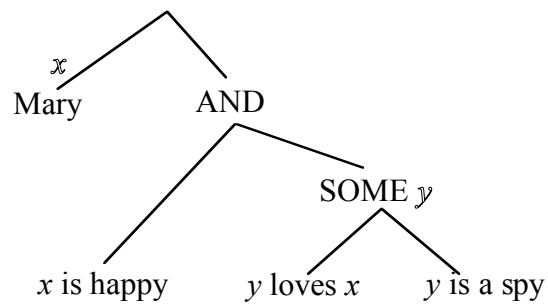
Some person is happy.

[  $(\text{Some } x: x \text{ is a person}) (x \text{ is happy})$  ]



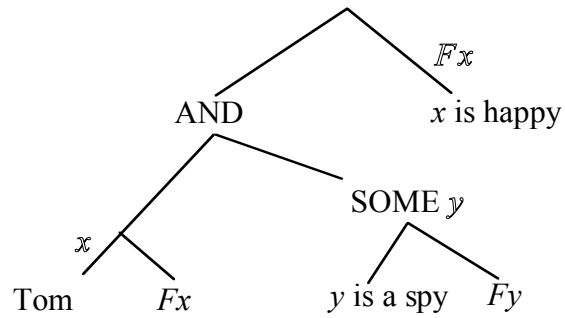
Mary is happy and some lover of hers is a spy.

[  $\forall x(x \text{ is happy and } (\text{some } y: y \text{ loves } x) (y \text{ is a spy})) (\text{Mary})$  ]

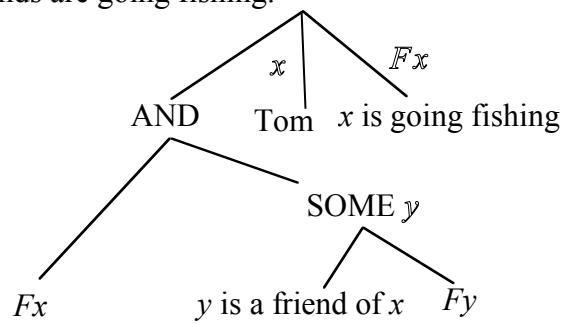


Tom and some spy are each happy.

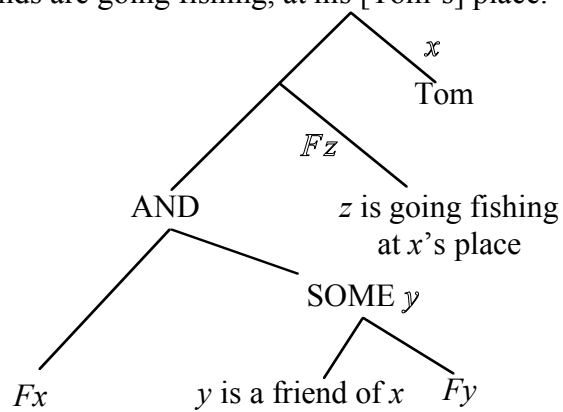
[  $\exists x(Fx \text{ and } (\exists y: y \text{ is a spy}) (y \text{ is } F)) (x \text{ is happy})$  ]



Tom and some of his friends are going fishing.

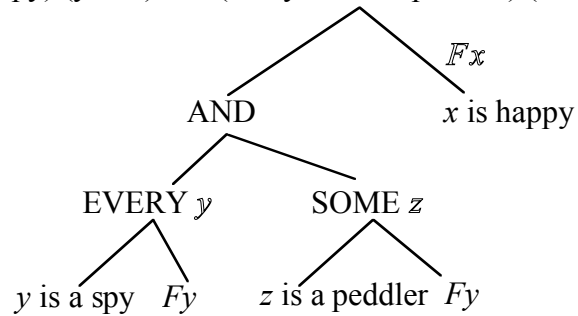


Tom and some of his friends are going fishing, at his [Tom's] place.



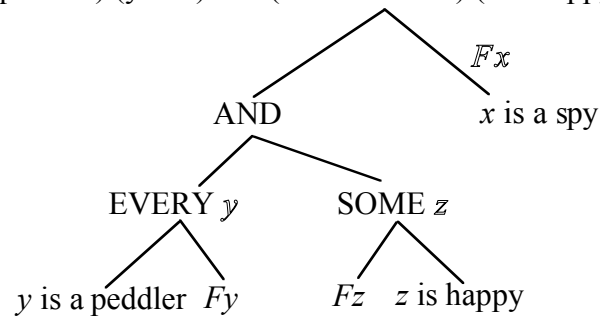
Every spy is happy, and some peddlers are too.

[  $\Box F$ ( every  $y$ :  $y$  is a spy) ( $y$  is  $F$ ) and (every  $z$ :  $z$  is a peddler) ( $z$  is  $F$ ) ) ( $x$  is happy) ]



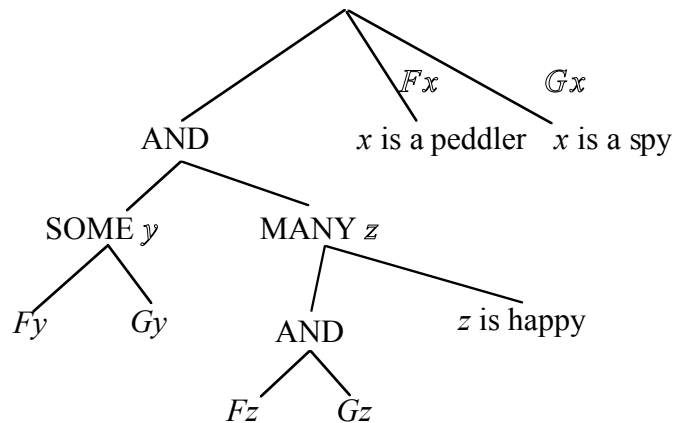
Spies are such that every peddler is one, and some of them [i.e. some spies] are happy.

[  $\Box F$ ( (every  $y$ :  $y$  is a peddler) ( $y$  is  $F$ ) and (some  $z$ :  $z$  is  $F$ ) ( $z$  is happy) ) ( $x$  is a spy) ]

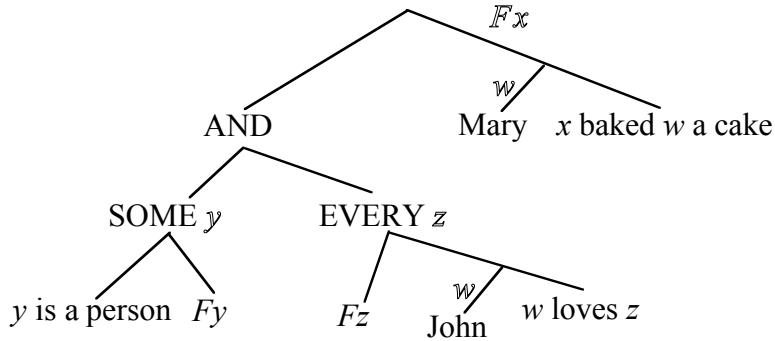


Some peddlers are spies, and many of them [the peddlers who are spies] are happy.

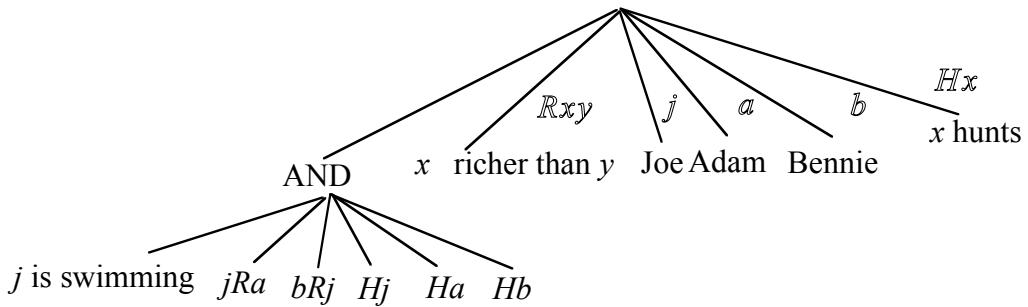
[  $\Box FG$ ( (some  $y$ :  $y$  is an  $F$ ) ( $y$  is  $G$ ) and (many  $z$ :  $z$  is  $F$  and  $z$  is  $G$ ) ( $z$  is happy) ) ( $x$  is peddler,  $x$  is a spy) ]



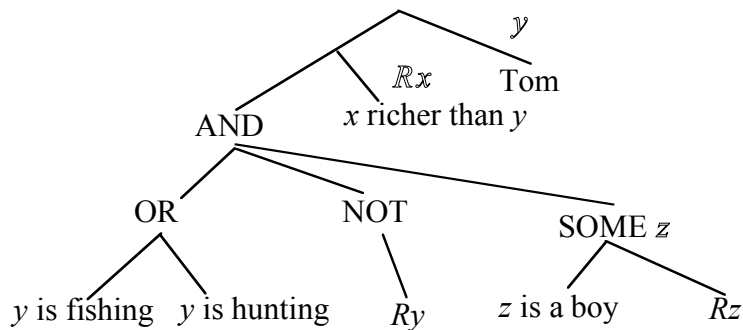
At least one person baked Mary a cake, and John loves everyone who did so.  
 [  $\exists F( (\text{some } y: y \text{ is a person}) (y \text{ is } F) \text{ and } (\text{every } z: z \text{ is } F) (\text{John loves } z) ) (x \text{ baked Mary a cake}) ]$



Joe is swimming, and he's more rich than Adam, but Bennie more [rich] than him, and all three hunt.



Tom is either fishing or hunting, and he's not richer than himself, but some boys are [richer than Tom].



Joe is swimming, and Tom is doing that and hunting Joe.

